STAT-IMM, a statistical approach to determine local and background contributions to PM$_{10}$ levels

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Abstract. When studying concentrations of particulate matter with a size of 10 $\mu$m or below (PM$_{10}$), measured locally, it becomes evident that two main portions need to be quantified: The concentration produced by sources in the vicinity of the station and the long range transports. The traditional approaches include analyses of the components of PM$_{10}$, comparisons upwind and downwind of a station, investigation of trajectories and complex chemical transport modelling. The development of an independent strategy which makes use of statistical methods, including regression and correlation analysis is a reasonable alternative. This method, presented here, does not apply the concept of PM$_{10}$ sources, but, rather, analyzes the relations between times series of PM$_{10}$ measurements and atmospheric properties. It is applied to identify the shares of the local portion and the large-scale background plus a stochastic portion that cannot be attributed to either of the two. Using regression analysis, a set of objectively chosen meteorological parameters is used to reconstruct the local PM$_{10}$ measurement series, defining the local portion. This weather-dependent part of the series is then removed and the residuum, which contains the large-scale PM$_{10}$ background and a stochastic portion is analyzed further with correlations. Results are shown for a three-year set of data which includes well over 250 PM$_{10}$ stations across Germany. The data is analyzed according to different stratifications, such as the PM$_{10}$ load and the wind direction as well as for the data set as a whole. In a further development of the method, a study of PM$_{10}$ transports across several border sections is shown.

1 Introduction

1.1 Demands on an assessment of PM$_{10}$ portions

The pollution load of particulate matter, both from local emissions and long range transports, constitutes a major problem in air quality. Meteorological conditions determine how the particles are transported and which concentrations are detected locally. In order to assess the effort/benefit ratio of regional and federal emission reduction measures in Germany, the share of measured concentrations of particulate matter of 10 $\mu$m or less (PM$_{10}$), advected from outside the country, is of major importance (EU, 1996; EU-Council, 1997; EU, 1999; Garber et al., 2002). Therefore, a major goal is to discern the average PM$_{10}$ portions local (I$_{L}$), large-scale background (I$_{B}$) and stochastic (I$_{S}$).

In the past there were numerous studies which aimed at the identification of local and background portions of pollutants, which often used a combination of physical and statistical methods, e.g., Merrill et al. (1985), Harris and Kahl (1990) or Oltmans et al. (1996). Studies, e.g., by Man and Shih (2001), van Dingenen et al. (2004), Querol et al. (2004) or Querol et al. (2007) were focusing on particulate matter. This study aims to complement them and offers a straightforward approach to discern the PM$_{10}$ portions.

Such an exercise should keep representativity in mind. Thus it should be able to produce results for a continuous time span and describe average conditions. It should furthermore aim at a description that can be verified by actual measurements. We are aware that PM$_{10}$ observations contain gaps and errors. A detailed investigation of these factors is given in Warnecke et al. (2006). Rigorous state-of-the-art quality control including homogenization and correction must be performed beforehand. It is acknowledged that after the application of these procedures there may be remanent systematic errors in the PM$_{10}$ levels but experience shows that the variability of the measurement errors is considerably lower. The method presented here focuses on regression and correlation which both evaluate variabilities rather than means.
All causes for potential errors notwithstanding, we argue that the use of PM$_{10}$ measurements is more effective than the determination of source strengths, because for the latter the processes that produce and convert PM$_{10}$ are not sufficiently known, wherefore a source-based PM$_{10}$ quantification has considerable error margins (Stern, 2006).

1.2 Approaches to PM$_{10}$ assessment

There are four main approaches to quantify what is produced in the vicinity and what is belonging to the background, possibly transported over longer distances.

- Laboratory analysis of PM$_{10}$ components (Stohl and Kromp-Kolb, 1994; Lenschow et al., 2001; Querol et al., 2004): This method is better suitable for PM$_{10}$ episodes than for an assessment of the mean state.

- Upwind/Downwind Method (Hainisch and Neubauer, 2004): Here, groups of measurements upwind and downwind of potential PM$_{10}$ sources are compared. This method has expedient aspects because it uses concentrations (that which is received at a measurement station), rather than emissions, i.e., source strengths which are very difficult to estimate (cf. Sect. 1.1).

- Trajectory analysis (Danielsen, 1974; Seibert, 1993): This method combines elements of the source-identifying laboratory analyses and the quantitative upwind/downwind approach by way of tracing the origin of PM$_{10}$ concentrations measured at a station. It is better suitable for single high-concentration episodes than for the assessment of an extended time span.

- Transport modelling (Yamartino et al., 1992; Stern, 2003, 2006): This set of approaches aims at a physically appropriate description of all PM$_{10}$-relevant processes. This very complex approach is highly dependent on a correct assumption of the magnitude of the PM$_{10}$ sources - prone to large uncertainties (cf. Sect. 1.1). As noted in van Loon et al. (2004) and Stern (2006), this is particularly visible in these models’ underestimation of measured high PM$_{10}$ concentrations.

It should be added that, for all approaches above, terms like “local”, “background”, “vicinity” or “long distance” are used by the respective authors as orientation categories rather than being attributable to fixed sizes. A definition according to the statistical method presented here is given in Sect. 3.3.

1.3 STAT-IMM, yet another method?

At first, a distinction of the German pollution terminology should be pointed out. It forms the word pair emission-immission in order to tell apart quantities that are produced and those which are arriving at a point of reference. Since “immission” is not part of the international terminology, we have resorted to the term “concentration” for the text. However, this emission-immission concept was also used for naming the PM$_{10}$ analysis method in German, hence it is called STAT-IMM, i.e., STATistical analysis of IMMission measurements. The method is based on a few key theses which link physical properties and mathematical/statistical concepts:

1. The variability (a second order moment) of a PM$_{10}$ series can, after minimizing the local PM$_{10}$ contribution, be separated into long-range transport and stochastical portion.

2. The terms large-scale background and long-range transport can be used in an equivalent way.

3. The correlation coefficient, when applied as in item 1 is the measure of the variability’s (percentual) fraction of the large-scale background;

4. The magnitude of the large-scale background can be linked to and expressed by the standard deviation of the series.

STAT-IMM evaluates solely concentrations, thus circumventing the problematic assessment of source strengths. It applies the statistical techniques of regression and correlation to a spatial set of PM$_{10}$ measurements. By themselves, these techniques are of course not novel but STAT-IMM applies them in a different setting, comprehensively described in Kreienkamp et al. (2007). They are employed to indirectly reconstruct local time series – a necessary step in assessing the local PM$_{10}$ component (by way of regression), to assess the magnitude of the long range transport (by way of correlation) and to separate long-range transport from stochastic fluctuations (also by way of correlation). Another important STAT-IMM feature is that it is not restricted to selected episodes – it addresses a continuous timeframe, for summer and winter separately.

2 Data

The following data types were used:

- Atmospheric three-dimensional climatology data from the NCEP-NCAR Reanalyses (Kalnay et al., 1996). Atmospheric data are supplying the predictors for the regression analysis and they are used for large-scale wind direction information.

- Air quality data from the data archive of the German Federal Environment Agency (UBA). 268 stations measuring PM$_{10}$ from 2001 to 2003 were used; half-hourly data were aggregated into hourly data, from which daily averages were computed. Data quality control and the supplement of missing data were carried out by the fully automated tool SYSTWARN (Kreienkamp and Enke, 2005).
– Air quality data from the AIRBase/AIRView web archive of the European Environment Agency (EEA), European Topic Center (ETC) for Air and Climate Change. 344 station time series from the Czech Republic, Austria, Switzerland, France and the Netherlands for the 2001-2003 period were selected. Quality control and the supplement of missing data were performed as with the German subset.

3 Method

3.1 Analysis of spurious correlations

Within STAT-IMM, spurious associations, such as annual and weekly cycles are identified and removed. The former is of no relevance to the results, since a large-scale, continuous data set is analyzed in which annual cycles are heterogeneous without phase consistency whilst the latter is subject to human-induced fluctuations (e.g. traffic or industry). The portion that can be attributed to the weekly cycle amounts to 3% of the total signal at most. This is a rather low figure due to the long, continuous time span analyzed, the high variability of weekly cycles and the effect that long range PM$_{10}$ transports may interfere with the weekly cycle.

3.2 Determination of the local portion of PM$_{10}$

The local portion ($I_L$) is identified first and then removed. To achieve this, a regression analysis is employed. Local time series of PM$_{10}$ are indirectly reconstructed by way of other properties, called predictors. The practise of determining relations between large scale atmospheric information and local measurements is well established, e.g., in the perfect prog approach (Klein, 1971; Kruizinga and Murphy, 1989) in statistical weather forecasting as well as in downscaling techniques for large-scale climate models (Enke and Spekat, 1997). The full set of potential predictors which is offered to the screening regression procedure would contain some 30 atmospheric parameters. This set, however, needs to be reduced, a step that is a necessary to achieve a regression based on local characteristics of the atmosphere. There are properties, such as the advection, which are by definition non-local and therefore have to be excluded from the set of predictors. We are aware that this is a compromise, because in principle all properties have a potential to improve the quality of the regression. However, the non-local predictors would be adding elements of ambiguity to the regression equation and thereby also diminish the efficiency of the procedure used to determine the large-scale background. In practise, out of the reduced pool of potential predictors the regression process objectively chooses the ones with the highest predictive power in a stepwise screening approach. Up to four of the potential predictors are allowed to be chosen for each station; a higher number would increase the danger of overfitting and numerical instability. The predictors which the screening regression selects most frequently are the thermal wind of the 850/1000 hPa layer, the geopotential gradient of the 500 hPa level and the temperature gradient in 850 hPa.

3.3 Determination of the large-scale background and the stochastic portion

Having quantified and removed the local PM$_{10}$ portion leaves the combination of $I_S+I_B$, the residual concentration, to be analyzed further. For a given station $X$, the correlations of the PM$_{10}$-series (having $I_L$ removed) with all others is computed. This results in a geographical distribution of correlations which is visualized as a map with colour-coded iso-correlates, as shown in Fig. 1a. The correlations are computed using a set of stations within and without Germany (cf. Sect. 2) of which only those in Germany or in close proximity to the border are graphed in the maps of this paper.

In order to derive the large-scale background, a qualitative and a quantitative argument is used. Let us begin with the qualitative reasoning. If we assume that the association between the time series at the reference station and all others were perfect, then the correlation coefficient would be equal to 1, i.e., the map displayed in Fig. 1a were entirely in dark green colour and there would be no stochastic component. Thus, whatever deviation from a correlation coefficient of 1 exists indicates the magnitude of the stochastic component.
This component includes, regardless of the small or large scale character of the signal (i) the asynchronous behaviour of the time series involved, (ii) PM$_{10}$ transformations, (iii) PM$_{10}$ sources and sinks and (iv) PM$_{10}$ mixing.

Let us now turn to the quantitative reasoning. It involves the definition of a so-called influence circle around the reference station which is indicated as a magenta ring in Fig. 1a. It is assumed that whatever remaining local influence there might be tapers off at a distance of 50 km from the reference station. The size of the circle is empirically determined as a balance between the minimization of local influences and retaining as much as possible of the large-scale background\footnote{Tests with different sizes of the circle showed that too small diameters would for some stations place too few reference points (i.e. other measuring stations) in its vicinity; enlarging the circle, on the other hand leads to an increasing stochastic portion and an artificial reduction of the target property: the large-scale background.}. In the iso-correlation map, the \textit{squared} correlation is averaged along this influence circle. This is necessary because the explained co-variance between measurement series is assessed. It should be pointed out that this procedure evaluates the correlation in the neighbourhood of the station outside the influence circle but ignores all correlation values from its immediate vicinity, i.e., from within the circle.

Therefore, the stochastic portion vanishes if the correlation coefficient along the influence circle equals 1; the large-scale background vanishes if the the correlations coefficient equals 0; the local portion vanishes if the mean total concentration at a station equals the standard deviation of the station’s series. The latter indeed happens but such cases are (i) extremely rare in the analyzed data set and (ii) indicate that the station is representative only for a very confined area because its PM$_{10}$-variability is extremely deviating from that in the surrounding area (example: a single, highly traffic-influenced station in a rural part of the network); Flemming et al. (2005) analyzed the spatial representativeness of different station types and developed a revised objective classification scheme for air quality regimes.

### 3.4 Example for the component separation

Here is an example using concentration data from a PM$_{10}$ station (Potsdam), taken between 2001 and 2003; the winter half-year is selected. A total average daily concentration $T_C$ of 29.2 $\mu$g/m$^3$ (=100%) occurred with a standard deviation $S_{dev}$ of 19.3 $\mu$g/m$^3$. The averaged (squared) correlation over the 50 km influence circle yielded a value of $R=0.79$.

- **Stochastic portion $I_S$:**
  $$(1-R)S_{dev}=4.1 \mu$g/m$^3$ or as a percentage $4.1/T_C \cdot 100=14\%.$$  

- **Large-scale background $I_B$:**
  $$R S_{dev}=15.2 \mu$g/m$^3$ or as a percentage $15.2/T_C \cdot 100=52\%.$$  

- **Local portion $I_L$:**
  $$T_C (I_S + I_L) = 9.9 \mu$g/m$^3$ or as a percentage $9.9/T_C \cdot 100=34\%.$$  

### 4 Results

#### 4.1 Signal strength assessment

An important first step is the assessment of the overall potential of detecting signals by way of correlation analysis. Figure 2 shows that correlation is not only indicative of the PM$_{10}$ large-scale background magnitude but can be used as well to determine in which regions strong signals can be expected at all. This is achieved by computing the correlation of all stations with all others (not, as in the other maps, of one station with all others) and extracting the long range transport portions as described in Sect. 3.4. The respective percentages for the average summer and winter conditions from the period 2001–2003 are graphed in Fig. 2.

The extended areas with a large-scale background portion of about 30% in summer and of 50% or more in winter indicate a good detectability of signals in the north half of Germany and, at least in the wintertime, in southern and eastern Bavaria, too. The seasonal difference in magnitude can be explained by a stronger atmospheric motion in winter which results in stronger transports.

Kreienkamp et al. (2007) give tables of $I_B$, $I_L$, $I_S$ and $T_C$ using STAT-IMM for a selection of German stations which aims at a good geographic coverage. $I_B$ tends to be in a range of 25–50%; the same range was found for these stations where $I_L$ and $I_S$ amount to 20–40%.
Table 1. Breakdown of the total PM$_{10}$ concentration (TC) into the large-scale background (IB), the local portion (IL) and the stochastic portion (IS) at station Braunschweig for 2001–2003 wintertime data. The three portions are displayed in terms of percentage and amount [$\mu$g/m$^3$]. The columns indicate if all winter days (all) or the classes very low (vlow), low, medium (med), high (hi) or very high (vhi) were used. The number of days in each class is given in parantheses. The tabulated information corresponds with the maps in Fig. 3.

<table>
<thead>
<tr>
<th></th>
<th>all (546)</th>
<th>vlow (171)</th>
<th>low (117)</th>
<th>med (81)</th>
<th>high (99)</th>
<th>vhi (78)</th>
</tr>
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<tbody>
<tr>
<td>TC $\mu$g/m$^3$</td>
<td>45.2</td>
<td>30.8</td>
<td>43.8</td>
<td>46.6</td>
<td>51.1</td>
<td>70.0</td>
</tr>
<tr>
<td>IB $\mu$g/m$^3$</td>
<td>12.0</td>
<td>16</td>
<td>14</td>
<td>14</td>
<td>17</td>
<td>30</td>
</tr>
<tr>
<td>10/3 $\mu$g/m$^3$</td>
<td>5.0</td>
<td>6.1</td>
<td>6.4</td>
<td>8.9</td>
<td>30</td>
<td>21.3</td>
</tr>
<tr>
<td>IL $\mu$g/m$^3$</td>
<td>21.2</td>
<td>61</td>
<td>62</td>
<td>62</td>
<td>57</td>
<td>49</td>
</tr>
<tr>
<td>10/3 $\mu$g/m$^3$</td>
<td>22</td>
<td>6.9</td>
<td>10.7</td>
<td>24</td>
<td>25</td>
<td>20</td>
</tr>
<tr>
<td>IS $\mu$g/m$^3$</td>
<td>12.0</td>
<td>6.9</td>
<td>24</td>
<td>11.3</td>
<td>25</td>
<td>20</td>
</tr>
<tr>
<td>10/3 $\mu$g/m$^3$</td>
<td>6.9</td>
<td>10.7</td>
<td>24</td>
<td>11.3</td>
<td>25</td>
<td>20</td>
</tr>
</tbody>
</table>

Figure 3. Map of the correlation of the residual (large-scale background plus stochastic portion) PM$_{10}$ time series at Station Braunschweig with all other stations. The subfigures display the concentration magnitudes: (a) very low; (b) low; (c) medium; (d) high; (e) very high and (f) all days, i.e., without magnitude differentiation. The three portions of the total concentration for each class are given in Table 1.

4.2 Dependence on concentration levels

For the following analyses we have picked the station Braunschweig, because it is located in the area with a strong overall signal (see Fig. 2 and Sect. 4.1) and it is closer to the geometric center of Germany, thus enabling a more uniform picture, e.g., with respect to advection. Figure 3 shows the correlation maps for wintertime PM$_{10}$ levels at this station, stratified by five classes and Table 1 shows the three concentration portions for the five classes.

In the top left corner of each subfigure a wind direction polar plot indicates the frequency distribution of the wind direction for the respective class. This PM$_{10}$ concentration/wind direction-relation can be assessed from Fig. 3 and Table 1, keeping in mind that the property analyzed to obtain Fig. 3 is the PM$_{10}$ residuum, i.e., after the removal of the local portion IL. Thus a combination of large-scale background and stochastic portion is retained. It should be added that the classification for the concentration magnitude...
is not station-based but groups days with the respective levels averaged over the whole northwest corner (north of 50N and west of 12E) of Germany.

- The (removed) local portion clearly dominates the time series with values around 50% and more.
- Even at a low residuum concentrations there are high correlations; in this value range the correlations tend to be strongly associated with the wind direction.
- With higher concentration levels the wind directions tends to be a factor of decreasing importance for the shape of the strong correlation maximum surrounding the station; yet, if there were no direction-dependence, this maximum would be perfectly circular.
- Whereas the local portion and the stochastic portion do not vary much there is almost a doubling of the large-scale background towards the highest concentration class. This behaviour is in conjunction with the wind direction-dependency of PM$_{10}$ concentrations (cf. Sect. 4.3) and can, at least in part, be explained by an above-average share of southeasterly winds for days with peak PM$_{10}$ concentrations.

4.3 Dependence on wind direction

When stratifying the data according to wind direction, problems arise because of the uneven distribution in the four quadrants which disallows a further differentiation, e.g., according to magnitude classes. The unevenness can already be deduced from the wind direction polar plot in Fig. 3 where the NW and SW sector are much more frequent than the NE and SE sectors. It turns out that southeasterly winds, i.e., in the most infrequent quadrant (less than 10% of all days) nevertheless are associated with the highest correlations. Yet, the shape of the correlation maximum is oriented away from and perpendicular to the SE quadrant. This underlines that wind direction and PM$_{10}$ concentrations are exhibiting a more complex linkage than one might be tempted to assume. Owing to the concept behind correlations, it also indicates that synchronous behaviour in PM$_{10}$ time series exists downwind, which points at the area of the station as a source of PM$_{10}$ variability. Consequently, the shape of the correlation maximum in the maps must be interpreted with caution.

4.4 Large-scale background and cross-border PM$_{10}$ transport

In principle, the correlation-based analysis of PM$_{10}$ concentrations is not restricted to an evaluation along the 50 km circle around the reference station. It was, indeed, carried out along stretches of the boundary, too, as shown in Fig. 1b. The example of station Schweinfurt is used because it has significant (the 95% significance level for correlations based on 500 values is, e.g., 0.09) cross-border large-scale background amounts for all border segments. In other areas of Germany, these amounts were significant only for a few segments. Stations in proximity to boundaries show that up to half of I$_B$ is linked to that boundary, but this behaviour tapers off with distance. This entire effect is best developed in Northern Germany where the overall signal magnitude is largest (cf. Sect. 4.1 and Fig. 2). In conjunction with the Alps or the French border, no strong large-scale background signals are detected.

A note of caution: Correlations, by themselves, cannot be used to conclude if transports take place from or towards an area. This is a consequence of the facts discussed in Sects. 4.2 and 4.3. However, in principle, it is possible to combine correlation results with a directional analysis, e.g., by examining them in conjunction with wind direction information. The limitations caused by the imperfect concentration/wind direction-linkage notwithstanding, an attempt was made to analyze the cross-border data stratified by wind direction and an example result is given in Table 2.

When comparing the tabulated values with the information from Fig. 2 it becomes clear that only the coastal and the Polish boundary segment bear potential for cross-boundary transports, due to the shape of the correlation maximum. There is a pronounced direction-dependency which can be seen, e.g., in the presence of the strongest coastal influence for the NW wind quadrant as well as in the absence of a coastal portion for the SE wind quadrant. The linkage to cross-boundary transport w.r.t. Poland is visible best when

Table 2. Cross-boundary analysis of large-scale background PM$_{10}$ concentrations for station Potsdam stratified by wind direction (columns). Tabulated is the Total Concentration (T$_C$), and, as percentage and in $\mu$g/m$^3$, the large-scale background (I$_B$) and the portion (of T$_C$) of the cross-boundary transport for the coastal (coa) and the Polish (pol) segment. Wintertime data from 2001–2003 have been used.

<table>
<thead>
<tr>
<th></th>
<th>Northeast</th>
<th>Northwest</th>
<th>Southwest</th>
<th>Southeast</th>
</tr>
</thead>
<tbody>
<tr>
<td>T$_C$</td>
<td>%</td>
<td>$\mu$g/m$^3$</td>
<td>%</td>
<td>$\mu$g/m$^3$</td>
</tr>
<tr>
<td>I$_B$</td>
<td>45</td>
<td>29.2</td>
<td>24.5</td>
<td>29.4</td>
</tr>
<tr>
<td>POL</td>
<td>11</td>
<td>13.2</td>
<td>13.6</td>
<td>12.2</td>
</tr>
<tr>
<td>COA</td>
<td>4</td>
<td>1.2</td>
<td>17.4</td>
<td>1.0</td>
</tr>
</tbody>
</table>
looking at the concentration levels in $\mu g/m^3$ where the SE quadrant exhibits the highest values. However, due to the relative proximity of the station to the Polish border, significant values are found for all wind directions.

5 Conclusions

5.1 General remarks and comparison with other studies

The statistical method STAT-IMM, which analyzes PM$_{10}$ concentrations rather than PM$_{10}$ emissions, has shown to be a workable approach to separate and quantify the three shares in PM$_{10}$ measurement series: Local portion, large-scale background and stochastic portion. These are are contained jointly in the PM$_{10}$ series. We do not claim that STAT-IMM yields a perfect separation – for example the local portion (expressed by the weather influence) can only be minimized and not fully excluded. However, the approach with its combination of regression and correlation constitutes an alternative to the established methods (see Sects. 1.2 and 5.1), relying neither on chemical nor on purely physical modelling.

There are but very few comprehensive studies in which the three PM$_{10}$ portions were determined for all of Germany. In Diegmann et al. (2006) (referred to as DEA06 hereafter) there is a compilation of $I_S$, $I_B$ and $I_L$ for 37 Stations. They are neither covering all of the country, nor was the DEA06 analysis carried out using a common timeframe. However, a key finding was that $I_B$ tends to be present in all series with a fraction of at least 30% and at most 70%. Another finding was that for 34 out of these 37 stations $I_B$ is the strongest contributor – rivalled for a subset of 10 stations by a traffic-related local contribution of comparable magnitude. $I_L$, termed “urban load” in DEA06 ranges from virtual non-existence to a fraction of over 40%, which is also the case for $I_S$, termed “additional load” in DEA06. The corresponding STAT-IMM results have been shown at the end of Sect. 4.1. Because the time frame and the detection regions of DEA06 and this study are not congruent, a full match of the magnitudes of the results can not be expected – in fact, taking the large-scale background as an example, STAT-IMM predominantly indicates lower portions.

An other study to compare some of the STAT-IMM results with is the Stern (2006) report (referred to as S06 hereafter). Its subject is the modelling – using the REM-CALGRID model – of cross-boundary transports of PM$_{10}$ and NO$_2$. S06 focuses on the concentrations that arrive from sources in Poland at twelve PM$_{10}$ stations in Berlin; its time frame is the year 2002. They were computed to be around 10% of the total PM$_{10}$ concentrations. This magnitude is matched by the STAT-IMM findings, although we used a longer time frame.

5.2 Evaluation

One topic that needs to be addressed is the robustness of the STAT-IMM results. Due to the short time span for which PM$_{10}$ data were available a cross validation which would have developed the statistical relations on a sub-period and applied them to the complementary sub-period was not possible. Yet precautions were taken with respect to the statistic stability. These include the log-transformation of the initial values to ensure a better approximation to Gaussian probability density functions as well as a limitation to a selection of up to four predictors in the screening regression.

Could the discrimination abilities of STAT-IMM with respect to the three PM$_{10}$ shares be enhanced if all potential predictors were to be used to determine the local portion? It would appear that in this case the weather factors were more fully taken into account. But, as explained in Sect. 3.2, using such an approach would blur the distinctions between local and large-scale weather influences and thus have a detrimental effect on the determination of the large-scale background.

However, there seems to be a potential “correlation sink” in the amount assigned to the stochastic portion, where some information might be buried due to the fact that correlations evaluate synchronous behaviour in the time series. Using lag correlations is not helpful since they are employing a fixed lag and whatever lagged behaviour might exist would be different for each station due to the varying distances. This effect would assign too much of the correlation to the stochastic side, thus overestimating the stochastic portion. Nevertheless, when prudently interpreting the statistical analyses it can be stated that, particularly for the large-scale background, there is a dependence on magnitude as well as on advection.

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